

evs | 27

The 27th INTERNATIONAL  
ELECTRIC VEHICLE  
SYMPOSIUM & EXHIBITION

BARCELONA  
17th-20th November 2013

# The Optimal Choice of Operating Points in Large Series Hybrids

Qian Bui and Peter Bauer

Department of Electrical Engineering

University of Notre Dame

Organized by



Hosted by



In collaboration with



Supported by



European  
Commission

# evs | 27

The 27th INTERNATIONAL  
ELECTRIC VEHICLE  
SYMPOSIUM & EXHIBITION

BARCELONA  
17th-20th November 2013

## OUTLINE:

1. Introduction
2. Brake specific fuel consumption (BSFC) characterization
3. Results
4. Example
5. Conclusion and Interpretations

Organized by



Hosted by

AVERE

MEVA



In collaboration with

EVAAP EDTA

Supported by



European Commission

## 1. Introduction

- Environmental concerns: emissions
- Fossil fuel reserves: limited reserves
- Economic considerations: price of oil
- Focus here: Large Series Hybrids (Diesel ICE)

Organized by



Hosted by



In collaboration with



Supported by



## 1. Introduction cont.



Organized by



Hosted by



In collaboration with



Supported by



## 1. Introduction cont.

- Usually:  
Power generated(t) = power needed(t)
- Efficiency of ICEs is highly dependent on power output
- The efficiency problem in current day ICEs:
  - frequent load changes
  - operation away from bsfc optimum

Organized by



Hosted by



In collaboration with



Supported by



European  
Commission

Alternatives possible with hybrid power generation units:

- Generate power at “average” power levels and buffer power mismatch.
- Use a 2 operating point scheme, with one OP being the bsfc minimum.
- Use multiple operating points to follow power trajectory or LP filtered power request.

Organized by



Hosted by



In collaboration with



Supported by



## 1. Introduction cont.

- Here: The 2 OP scheme, with one OP being the bsfc optimum
- The other OP needs to be found
- Many advantages over the “average power” approach:
  - can be significantly more efficient
  - less storage requirement
  - average power sometimes unknown a priori making the approach difficult to apply

Organized by



Hosted by



In collaboration with



Supported by



## 2. Brake Specific Fuel Consumption Characterization

- BSFC are often given as isoclines of constant values in a torque-speed or power-speed diagram
- There exist infinitely many operating points that produce the same amount of power
- The function  $bsfc(P)$  maps  $P$  to the minimal achievable  $bsfc$  value for that power  $P$
- Typical functions  $bsfc(P)$  have a pronounced minimum at mid power levels and are continuous and differentiable in power

Organized by



Hosted by



In collaboration with



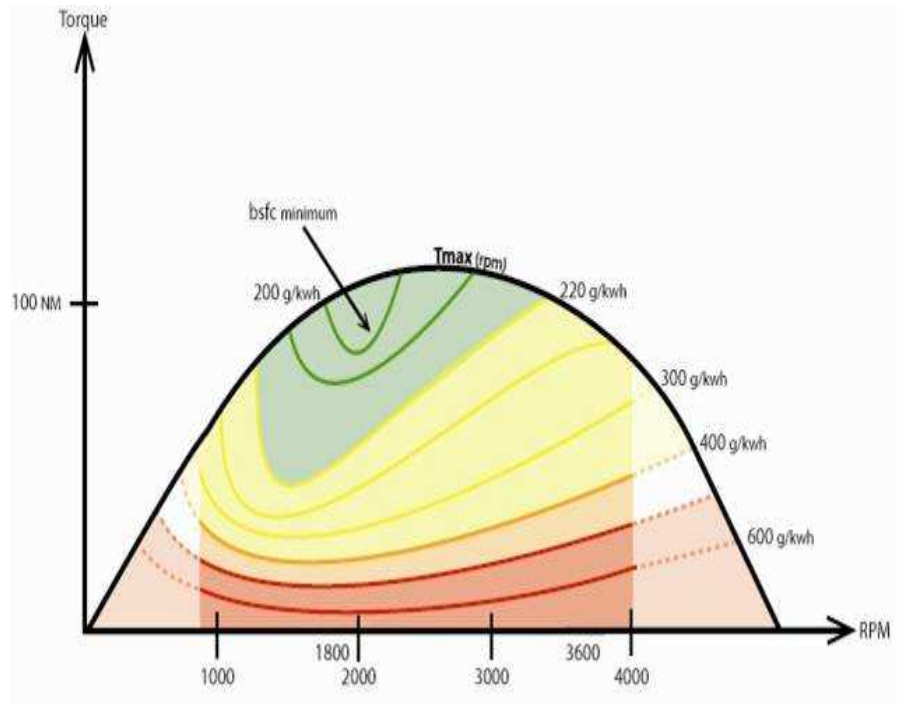
Supported by



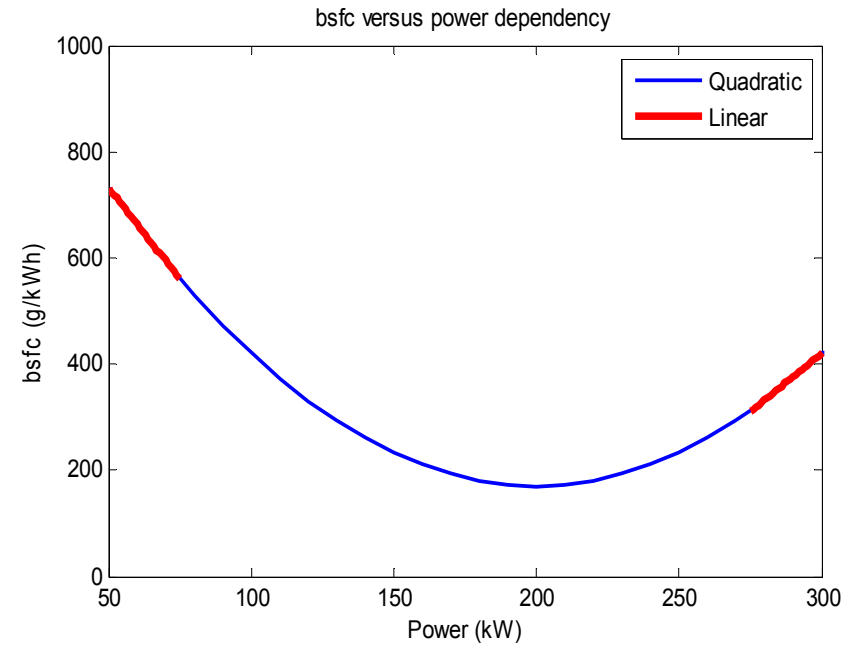


## 2. BSFC Characterization cont.

### Typical bsfc Representation



### BSFC(P)



Organized by



Hosted by



In collaboration with



Supported by



### Assumptions made:

- Quadratic bsfc dependency around bsfc minimum
- Linear dependency at very low and very high power
- No transient fuel consumption effects between Ops, i.e. long stay times.
- Many assumptions will be relaxed later

Organized by



Hosted by



In collaboration with



Supported by



European  
Commission

## 3. Results

Fuel mass consumed using a weighted average between average power OP and the two OP scheme:

$$M = T(q P1 \text{ bsfc}(P1) + q Popt \text{ bsfc}(Popt) + (1 - 2q) Pav \text{ bsfc}(Pav))$$

Where  $0 < q < 0.5$

P1: low operating point power

Popt: optimal operating point power

Pav: average power

M: fuel mass

T: engine run time

Organized by



Hosted by



In collaboration with



Supported by



## 3. Results

- For the two OP scheme to burn less fuel we need:

$$dM/dq < 0$$

- Remember:

$q=0$  means only  $P_{av}$  is used

$q=0.5$  means only  $(P_{opt}, P1)$  used

Also:  $P1 < P_{av} < P_{opt}$

Organized by



Hosted by



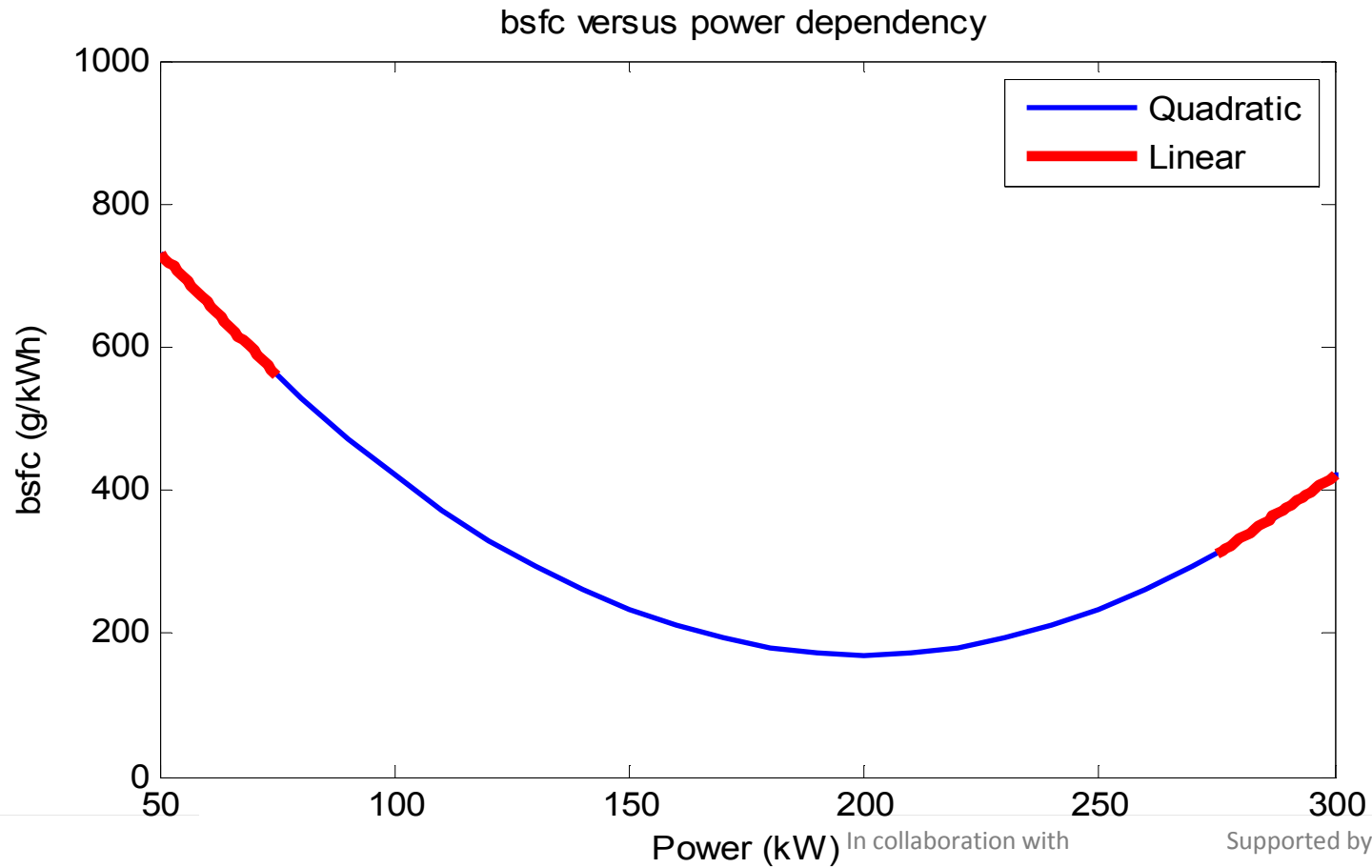
In collaboration with



Supported by



## 3. Results – BSFC Approximation



Organized by



In collaboration with



Supported by



- The Linear Case:

$$dM/dq < 0 \text{ if } P1 - P_{opt} < 0$$

which by definition is always satisfied.

=> If  $(P1, P_{av}, P_{opt})$  lie on a line with negative slope (linear case), cycling using  $P1$  and  $P_{opt}$  is always advantageous.

Organized by



Hosted by



In collaboration with



Supported by



European Commission

- The quadratic case:

$$dM/dq < 0 \quad \text{if} \quad 2P1 - P_{av} < 0$$

- This implies:

$$P1 < P_{av}/2 \quad \text{and} \quad P_{opt} - P_{av} > P1$$

Under these conditions cycling using (P1 and Popt) is advantageous.

Organized by



Hosted by



In collaboration with



Supported by



- The sub-linear case:  
meaning that  $P1$  is below the line of negative slope given by  $P_{opt}$  and  $P_{av}$ .  
=> Results are the same as for linear case – it is always advantageous to cycle !
- The sub-quadratic case:  
meaning that  $P1$  is below the quadratic dependency and above the linear one.  
=> Quadratic case results still hold!

Organized by



Hosted by



In collaboration with



Supported by





## 4. Example (Sub-quadratic case) 650KW Diesel Genset

- $P_{av} = 210\text{KW}$ ,  $bsfc = 240 \text{ g/Kwh}$
- $P_{opt} = 400\text{KW}$ ,  $bsfc = 180 \text{ g/Kwh}$
- $P_1 = 20\text{KW}$ ,  $bsfc = 320 \text{ g/Kwh}$
- Fuel consumption per hour at  $P_{av}$ : 50.4 Kg
- Fuel consumption per hour cycling between  $P_1$  and  $P_{opt}$ : 39.2Kg
- Fuel savings in one year (operating 80% of year):  
78490 kg = approx. 95000 liter of Diesel => between  
\$100,000 and \$3,000,000 depending on application

Organized by



Hosted by



In collaboration with



Supported by



## 5. Conclusion and Interpretations

- Conditions under which cycling in large series hybrids is advantageous
- In the linear negative slope bsfc case, it is always advantageous to cycle.
- In the quadratic case, cycling is advantageous if the low power OP is sufficiently small in power.
- Other dependencies were also investigated

Organized by



Hosted by



In collaboration with



Supported by



European Commission

## 5. Conclusion.....

- Note that “quadratic” and “linear” does not mean that the entire bsfc curve or even a part of it needs to be quadratic or linear, only the 3 points P1, Popt and Pav need to have this relationship!!
- Transient fuel consumption effects were not considered – long stay times assumed!
- Fuel savings can be large, typically 20 - 30%
- The results also apply to slowly time-variant average power

Organized by



Hosted by



In collaboration with



Supported by



### Open Problems and Questions:

- ⇒ Considering transient OP phenomena and their effects on fuel savings
- ⇒ Comparison with low pass filtered power request
- ⇒ A cost analysis of fuel savings versus hardware cost for storage.

Organized by



Hosted by



In collaboration with



Supported by



- For questions, comments or ideas:  
(Comentarios, preguntas, ideas?)

Peter Bauer

[pbauer@nd.edu](mailto:pbauer@nd.edu)

(001) 574 631 8015

Organized by



Hosted by



In collaboration with



Supported by



European  
Commission